

PAP Geometry Systems Notes

Name: Key

Determine the solution to the system of equations using the graphing method.

1.
$$\begin{cases} y = \frac{1}{2}x + 4 \\ y = 6x - 1 \end{cases}$$

$(\frac{10}{11}, 4.5)$

$\frac{1}{2}x + 4 = 6x - 1$ (use calc)
 $-\frac{1}{2}x + 1 \quad -\frac{1}{2}x + 1$
 $5 = 5.5x$
 $\frac{5}{5.5} = \frac{5.5x}{5.5}$
 $x = \frac{10}{11} \quad y = 4.45$

Determine the solution to the system of equations using the substitution method.

2.
$$\begin{cases} y = -2 \\ 4x - 3y = 18 \end{cases}$$

$4x - 3(-2) = 18$
 $4x + 6 = 18$
 $-6 \quad -6$
 $4x = 12$
 $x = 3$

$(3, -2)$

Determine the solution to the system of equations using the elimination method.

3.
$$\begin{cases} -4x - 2y = -12 \\ 4x + 8y = -24 \end{cases}$$

$6y = -36$
 $y = -6$

$-4x - 2(-6) = -12$
 $-4x + 12 = -12$
 $-4x = -24$
 $x = 6$

$(-6, 6)$

Determine the solution to the system of equations using ANY method.

4.
$$\begin{cases} 2x + 16y = 64 \\ x = 8y \end{cases}$$

$2(8y) + 16y = 64$
 $16y + 16y = 64$
 $32y = 64$
 $\frac{32y}{32} = \frac{64}{32}$
 $y = 2$

$x = 8(2)$
 $x = 16$

$(16, 2)$

Solving Systems of Equations by Elimination

Date _____ Period _____

Solve each system by elimination.

~~$$\begin{aligned} 1) \quad -4x - 2y &= -12 \\ 4x + 8y &= -24 \end{aligned}$$~~

$$\begin{aligned} 2) \quad 4x + 8y &= 20 \\ -4x + 2y &= -30 \\ \hline 10y &= -10 \\ y &= -1 \end{aligned}$$

$$\begin{aligned} 4x + 8(-1) &= 20 \\ 4x - 8 &= 20 \\ 4x &= 28 \\ x &= 7 \end{aligned}$$

$$\boxed{(7, -1)}$$

$$\begin{aligned} 3) \quad x - y &= 11 \\ 2x + y &= 19 \\ \hline 3x &= 30 \\ x &= 10 \end{aligned}$$

$$\begin{aligned} 10 - y &= 11 \\ -y &= 1 \\ y &= -1 \end{aligned}$$

$$\boxed{(10, -1)}$$

$$\begin{aligned} 4) \quad -6x + 5y &= 1 \\ 6x + 4y &= -10 \\ \hline 9y &= -9 \\ y &= -1 \end{aligned}$$

$$\boxed{(-1, -1)}$$

$$\begin{aligned} 6x + 4(-1) &= -10 \\ 6x - 4 &= -10 \\ +4 \quad +4 & \\ 6x &= -6 \\ x &= -1 \end{aligned}$$

$$\begin{aligned} 6) \quad 8x + y &= -16 \\ -(-3x + y) &= -5 \\ \hline 8x + y &= -16 \\ 3x - y &= 5 \\ \hline 11x &= -11 \\ x &= -1 \end{aligned}$$

$$\begin{aligned} 8(-1) + y &= -16 \\ -8 + y &= -16 \\ y &= -8 \end{aligned}$$

$$\boxed{(-1, -8)}$$

$$\begin{aligned} 8) \quad 7x + 2y &= 24 \\ 8x + 2y &= 30 \\ \hline -x &= -6 \\ x &= 6 \end{aligned}$$

$$\begin{aligned} 8(6) + 2y &= 30 \\ 48 + 2y &= 30 \\ 2y &= -18 \\ y &= -9 \end{aligned}$$

$$\boxed{(6, -9)}$$

$$\begin{aligned} 10) \quad -4x + 9y &= 9 \\ 3(x - 3y) &= -6 \\ \hline -4x + 9y &= 9 \\ 3x - 9y &= -6 \\ \hline -x &= -9 \\ x &= 9 \end{aligned}$$

$$\begin{aligned} 9 - 3y &= -6 \\ -3y &= -15 \\ y &= 5 \end{aligned}$$

$$\boxed{(9, 5)}$$

$$\begin{aligned} 12) \quad -7x + y &= -19 \\ -2x + 3y &= -19 \\ \hline -7x + y &= -19 \\ -2x + 3y &= -19 \\ \hline -5x - 2y &= 0 \end{aligned}$$

$$\begin{aligned} -2(-4) + 3y &= -19 \\ 8 + 3y &= -19 \\ 3y &= -27 \\ y &= -9 \end{aligned}$$

$$\begin{aligned} 19x &= -76 \\ x &= -4 \end{aligned}$$

$$\boxed{(-4, -9)}$$

$$\begin{aligned} 5) \quad -2x - 9y &= -25 \\ -1(-4x - 9y) &= -23 \\ \hline -2x - 9y &= -25 \\ 4x + 9y &= 23 \\ \hline 2x &= -2 \\ x &= -1 \end{aligned}$$

$$\begin{aligned} -2(-1) - 9y &= -25 \\ 2 - 9y &= -25 \\ -9y &= -27 \\ y &= 3 \end{aligned}$$

$$\boxed{(-1, 3)}$$

$$\begin{aligned} 7) \quad -6x + 6y &= 6 \\ -6x + 3y &= -12 \\ \hline 3y &= 18 \\ y &= 6 \end{aligned}$$

$$\begin{aligned} -6x + 6(6) &= 6 \\ -6x + 36 &= 6 \\ -6x &= -30 \\ x &= 5 \end{aligned}$$

$$\boxed{(5, 6)}$$

$$\begin{aligned} 9) \quad 5x + y &= 9 \\ 10x - 7y &= -18 \\ \hline 5x + y &= 9 \\ -10x - 2y &= -18 \\ \hline -5x - 3y &= -9 \\ 5x + y &= 9 \\ \hline -2y &= 0 \\ y &= 0 \end{aligned}$$

$$\begin{aligned} 5x + 0 &= 9 \\ 5x &= 9 \\ x &= 1.8 \end{aligned}$$

$$\boxed{(1.8, 0)}$$

$$\begin{aligned} 11) \quad -3x + 7y &= -16 \\ -9x + 5y &= 16 \\ \hline -3x + 7y &= -16 \\ -9x + 5y &= 16 \\ \hline 6x - 2y &= -32 \\ -3x + 7y &= -16 \\ \hline 9y &= -16 \\ y &= -1.78 \end{aligned}$$

$$\begin{aligned} -3x + 7(-1.78) &= -16 \\ -3x - 12.46 &= -16 \\ -3x &= -3.54 \\ x &= 1.18 \end{aligned}$$

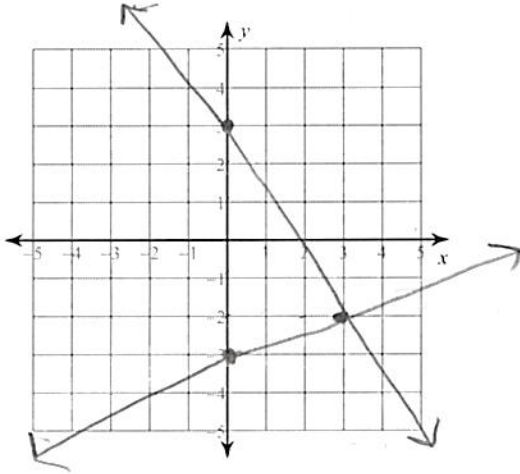
$$\boxed{(1.18, -1.78)}$$

Solving Systems of Equations by Graphing

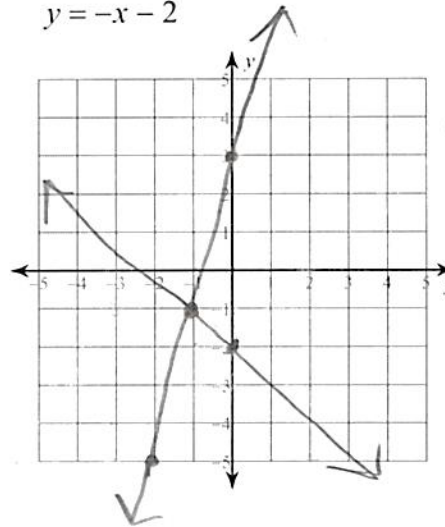
Solve each system by graphing.

1) $y = -\frac{5}{3}x + 3$

$y = \frac{1}{3}x - 3$

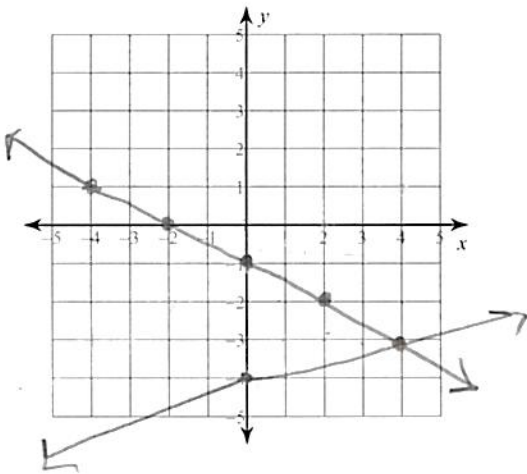
 $(3, -2)$ 

2) $y = 4x + 3$
 $y = -x - 2$

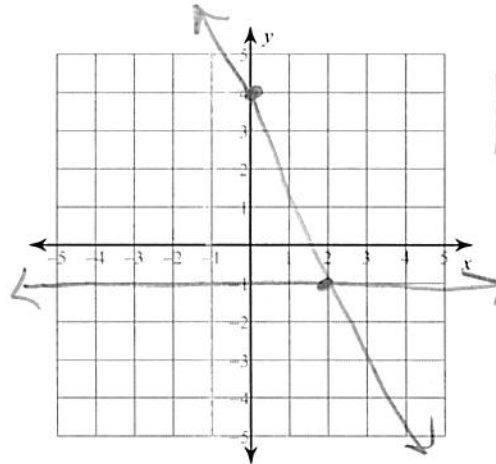
 $(-1, -1)$ 

3) $y = -\frac{1}{2}x - 1$

$y = \frac{1}{4}x - 4$

 $(4, -3)$ 

4) $y = -1$
 $y = -\frac{5}{2}x + 4$

 $(2, -1)$ 

Solving Systems of Equations by Substitution

Date _____ Period _____

Solve each system by substitution.

$$\begin{aligned}
 1) \quad y &= 6x - 11 & y &= 6(2) - 11 \\
 -2x - 3y &= -7 & &= 12 - 11 \\
 -2x - 3(6x - 11) &= -7 & &= 1 \\
 -2x - 18x + 33 &= -7 \\
 -20x &= -40 & \boxed{(2, 1)} \\
 x &= 2
 \end{aligned}$$

$$\begin{aligned}
 2) \quad 2x - 3y &= -1 & y &= 4 - 1 \\
 y &= x - 1 & & y = 3 \\
 2x - 3(x - 1) &= -1 \\
 2x - 3x + 3 &= -1 \\
 -x &= -4 & \boxed{(4, 3)} \\
 x &= 4
 \end{aligned}$$

$$\begin{aligned}
 3) \quad y &= -3x + 5 & y &= -3(1) + 5 \\
 5x - 4y &= -3 & & y = 2 \\
 5x - 4(-3x + 5) &= -3 & & \\
 5x + 12x - 20 &= -3 \\
 17x &= 17 & \boxed{(1, 2)} \\
 x &= 1
 \end{aligned}$$

$$\begin{aligned}
 4) \quad -3x - 3y &= 3 \\
 y &= -5x - 17 \\
 -3x - 3(-5x - 17) &= 3 \\
 -3x + 15x + 51 &= 3 \\
 12x &= -48 \\
 \boxed{x = -4}
 \end{aligned}$$

$$\begin{aligned}
 5) \quad y &= -2 \\
 4x - 3y &= 18
 \end{aligned}$$

$$\begin{aligned}
 6) \quad y &= 5x - 7 & y &= 5(2) - 7 \\
 -3x - 2y &= -12 & & y = 10 - 7 \\
 -3x - 2(5x - 7) &= -12 & & y = 3 \\
 -3x - 10x + 14 &= -12 \\
 -13x &= -26 & \boxed{(2, 3)} \\
 x &= 2
 \end{aligned}$$

$$\begin{aligned}
 7) \quad -4x + y &= 6 & y &= 4x + 6 \\
 -5x - y &= 21 \\
 -5x - (4x + 6) &= 21 & y &= 4(3) + 6 \\
 -5x - 4x - 6 &= 21 & & y = -12 + 6 \\
 -9x &= 27 & & y = -6 \\
 x &= -3 & \boxed{(-3, -6)}
 \end{aligned}$$

$$\begin{aligned}
 8) \quad -7x - 2y &= -13 & -7(2y + 11) - 2y &= -13 \\
 x - 2y &= 11 & & -14y - 77 - 2y = -13 \\
 x &= 2y + 11 & & -16y = 64 \\
 x &= 2(-4) + 11 & & -16y = 64 \\
 x &= -8 + 11 & & y = -4 \\
 x &= 3 & \boxed{(3, -4)}
 \end{aligned}$$

$$\begin{aligned}
 9) \quad -5x + y &= -2 & y &= 5x - 2 \\
 -3x + 6y &= -12 \\
 -3x + 6(5x - 2) &= -12 \\
 -3x + 30x - 12 &= -12 \\
 27x &= 0 & y &= 5(0) - 2 \\
 x &= 0 & & y = -2 \\
 \boxed{(0, -2)}
 \end{aligned}$$

$$\begin{aligned}
 10) \quad -5x + y &= -3 & y &= 5x - 3 \\
 3x - 8y &= 24 \\
 3x - 8(5x - 3) &= 24 \\
 3x - 40x + 24 &= 24 \\
 -37x &= 0 \\
 x &= 0 & y &= 5(0) - 3 \\
 \boxed{(0, -3)} & & & y = -3
 \end{aligned}$$